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What is claimed is:

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A method of determining value-at-risk, comprising the steps of:

electronically receiving financial market transaction data over an electronic network;

electronically storing in a computer-readable medium said received financial market transaction data;

constructing an inhomogeneous time series z that represents said received financial market transaction data:

constructing an exponential moving average operator;

10 constructing an iterated exponential moving average operator based on said exponential moving average operator;

constructing a time-translation-invariant, causal operator $\Omega[z]$ that is a convolution operator with kernel ω and that is based on said iterated exponential moving average operator;

electronically calculating values of one or more predictive factors relating to said time series z, wherein said one or more predictive factors are defined in terms of said operator $\Omega[z]$;

electronically storing in a computer readable medium said calculated values of one or more predictive factors; and

electronically calculating value-at-risk from said calculated values.

The method of claim 1, wherein said operator Ω[z] has the form:

$$\Omega[z](t) = \int_{-\infty}^{t} dt' \omega(t-t') z(t')$$

$$= \int_{0}^{\infty} dt' \omega(t') z(t-t').$$
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The method of claim 1, wherein said exponential moving average operator
 EMA[\tau: z] has the form:

EMA[
$$\tau, z$$
] $(t_n) = \mu$ EMA(τ, z] $(t_{n-1}) + (\nu - \mu) z_{n-1} + (1 - \nu) z_n$, with
$$\alpha = \frac{\tau}{t_n - t_{n-1}},$$

$$\mu = e^{-\alpha}$$
(23)

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where ν depends on a chosen interpolation scheme.

4. The method of claim 1, wherein said operator $\Omega[z]$ is a differential operator

5 $\Delta[\tau]$ that has the form:

$$\Delta[\tau] = \gamma(\text{EMA}[\alpha\tau, 1] + \text{EMA}[\alpha\tau, 2] - 2 \text{ EMA}[\alpha\beta\tau, 4]),$$

where γ is fixed so that the integral of the kernel of the differential operator from the origin to the first zero is 1; α is fixed by a normalization condition that requires $\Delta[\tau; c] = 0$ for a constant c; and β is chosen in order to get a short tail for the kernel of the differential operator $\Delta[\tau]$.

- 5. The method of claim 4 wherein said one or more predictive factors comprises a return of the form $r[\tau] = \Delta[\tau; x]$, where x represents a logarithmic price.
- 6. The method of claim 1 wherein said one or more predictive factors comprises a momentum of the form $x \text{EMA}[\tau; x]$, where x represents a logarithmic price.
- The method of claim 1 wherein said one or more predictive factors comprises a volatility.
 - The method of claim 7 wherein said volatility is of the form:

Volatility
$$[\tau, \tau', p; z] = MNorm [\tau/2, p; \Delta[\tau'; z]],$$
 where

$$MNorm[\tau, p; z] = MA[\tau; |z|^p]^{1/p}$$
, and

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$$\operatorname{MA}[\tau,n] = \frac{1}{n} \sum_{k=1}^{n} \operatorname{EMA}[\tau',k],$$
 with $\tau' = \frac{2\tau}{n+1}$, and where p satisfies $0 , and τ' is a time horizon of a return $r[\tau] = \Delta[\tau; x]$, where x represents a logarithmic price.$

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